

Surname \_\_\_\_\_

Forename(s) \_\_\_\_\_

Candidate signature \_\_\_\_\_

I declare this is my own work.

# GCSE MATHEMATICS

Higher Tier

Paper 2 Calculator

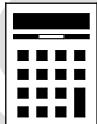
Shadow paper based on November 2021 question paper

Time allowed: 1 hour 30 minutes

**Materials**

For this paper you must have:

- a calculator
- mathematical instruments.

**Instructions**

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Fill in the boxes at the top of this page.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- If you need extra space for your answer(s), use the lined pages at the end of this book. Write the question number against your answer(s).
- Do all rough work in this book. Cross through any work you do not want to be marked.

**Information**

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

**Advice**

In all calculations, show clearly how you work out your answer.

For Examiner's Use	
Pages	Mark
2–3	
4–5	
6–7	
8–9	
10–11	
12–13	
14–15	
16–17	
18–19	
20–21	
22–23	
24	
<b>TOTAL</b>	

Answer **all** questions in the spaces provided.

Do not write  
outside the  
box

1 Circle the factor of  $x^2 + 2x$

[1 mark]

$x + 1$

$-2x$

$x + 2$

$2x$

2  $B$  is one third of  $A$ .

Work out the ratio  $A : B$

Circle your answer.

[1 mark]

$1 : 3$

$3 : 1$

$1 : 4$

$4 : 1$

3 The first three terms of a geometric progression are  $\frac{2}{5}$   $\frac{4}{25}$   $\frac{8}{125}$

Circle the fourth term.

[1 mark]

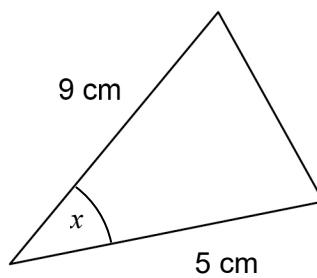
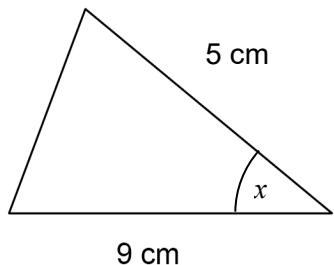
$\frac{10}{625}$

$\frac{12}{625}$

$\frac{16}{625}$

$\frac{32}{625}$

4

Not drawn  
accurately

Circle the reason why these triangles are congruent.

[1 mark]

ASA

RHS

SAS

SSS

5

Solve  $12x = 98.8 - 7x$ 

[2 marks]

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 $x =$  \_\_\_\_\_

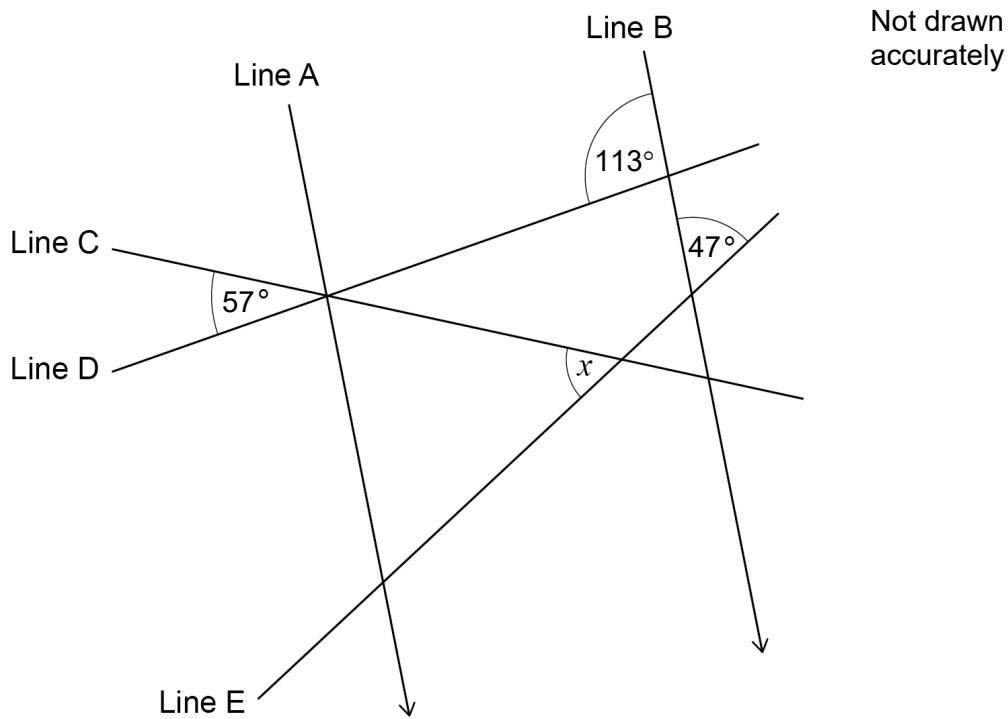
6

Turn over ►

6

Lines A, B, C, D and E intersect as shown.

Lines A and B are parallel.



Work out the size of angle  $x$ .

[3 marks]

Answer degrees

7

112 women and 95 men from Bolton went clothes shopping in February.

The table shows information about the mean amount spent, in pounds, by each person.

Do not write  
outside the  
box

	Women	Men
Number of people	112	95
Mean amount spent (£)	68.50	52.40

The national mean for clothes spending per person in February was £63.

Was the mean spend for the people in Bolton greater than the national mean in February?

You **must** show your working.

**[3 marks]**

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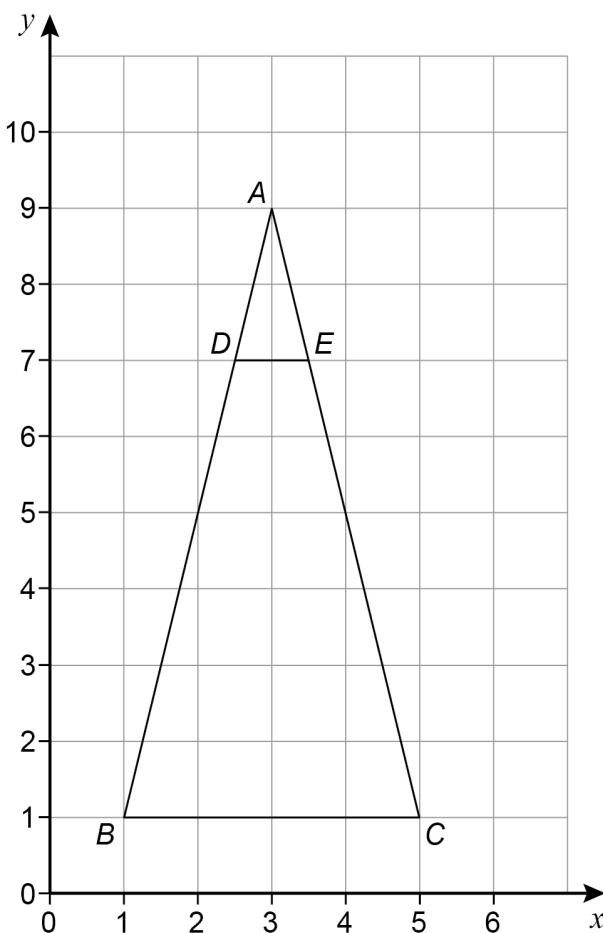


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6

**Turn over ►**

8



Describe fully the **single** transformation that maps triangle  $ADE$  to triangle  $ABC$ .

[3 marks]

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9 A ball contains  $3000 \text{ cm}^3$  of air.

More air is pumped into the ball at a rate of  $500 \text{ cm}^3$  per second.

The ball is full of air when it becomes a sphere with radius 20 cm



Volume of a sphere =  $\frac{4}{3}\pi r^3$  where  $r$  is the radius

Does it take **less than** 1 minute to fill the ball?

You **must** show your working.

[4 marks]

10

*a* is a negative number.

*b* is a negative number.

For each statement, tick the correct box.

[4 marks]

## Always true

## Sometimes true

**Never true**

$a + b$  is positive

1

1

1

$a - b$  is positive

1

1

1

$a^2 + b^2$  is positive

1

$a^3 \div b^3$  is positive

1

1

11 250 trains arrived at a station.

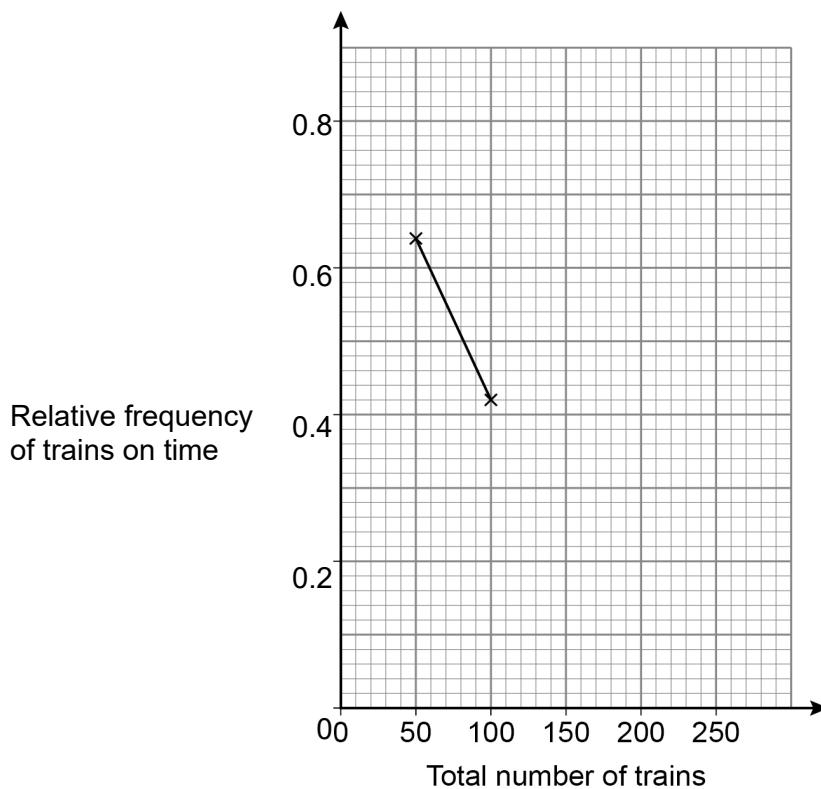
The number of trains that were on time was recorded after every 50 trains.

The table shows some information about the results.

<b>Total number of trains</b>	50	100	150	200	250
<b>Total number of trains on time</b>	32	42	108	160	185
<b>Relative frequency of trains on time</b>	0.64	0.42			

11 (a) Complete the relative frequency graph.

[3 marks]



11 (b) Write down the best estimate of the probability that a train arriving at the station is on time.

[1 mark]

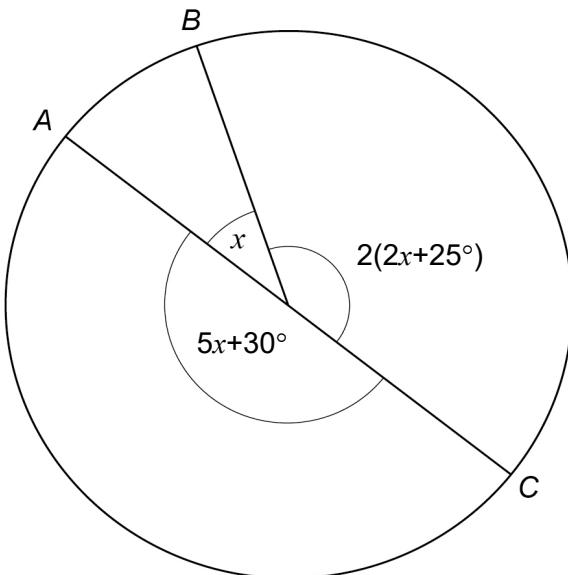
Answer \_\_\_\_\_

12

*A, B and C are three points on a circle.*

The radii from  $A$ ,  $B$  and  $C$  are shown.

Not drawn accurately



Is AC a diameter of the circle?

You **must** show your working.

[3 marks]

## 13 A straight line

has gradient 5

and

passes through the point  $(3, 11)$

Work out the equation of the line.

Give your answer in the form  $y = mx + c$

[3 marks]

## Answer

**Turn over for the next question**

14 The population of moths in a park is 5800

14 (a) Assume that the population increases by 15% each day.

Show that after 12 days the population would be greater than 30 000

[2 marks]

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14 (b) In fact, the population increases by 17% each day for 11 days then decreases by 9% for 1 day.

After the 12 days, is the actual population greater than 30 000 ?

Tick a box

1

Yes

1

No

Show working to support your answer.

[2 marks]

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14 (c) The expected number of visitors to the park each day depends on the temperature.

Temperature	Expected number of visitors each day
Less than 20°C	500
20°C or more	700

On each of the 31 days in July

the park is open

the probability that the temperature is less than 20°C is 0.3

Work out the **total** number of expected visitors to the park in July.

[3 marks]

### Answer

15  $y$  is inversely proportional to  $x^2$   
 $y = 6$  when  $x = 2$

**15 (a)** Work out an equation connecting  $y$  and  $x$ .

[3 marks]

### Answer

**15 (b)** Work out the value of  $y$  when  $x = 5$

**[2 marks]**

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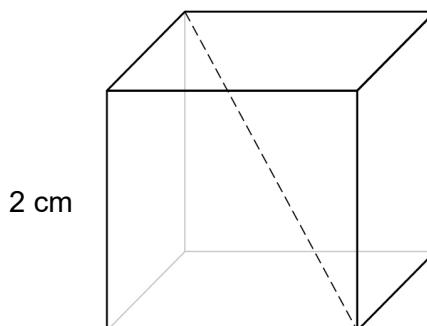
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### Answer

**16**

Here is a cube with edge length 2 cm

One diagonal is shown.

**16 (a)** Circle the length, in centimetres, of the diagonal.**[1 mark]**

$\sqrt{6}$	$\sqrt{8}$	$\sqrt{12}$	8
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**16 (b)** The total length, in centimetres, of the edges of a different cube is a multiple of 24

Circle the correct statement.

**[1 mark]**

The length of each side is a whole number	The length of each side is <b>not</b> a whole number	The length of each side <b>might</b> be a whole number
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**Turn over for the next question**

17 30 people were asked which public transport they used more often, bus or train. The table shows the results.

	Bus	Train
Male	4	10
Female	9	7

17 (a) One male and one female are chosen at random.

Work out the probability that **exactly** one of them said bus.

[3 marks]

## Answer

**17 (b)** Two males are chosen at random.

Work out the probability that they **both** said train.

[2 marks]

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## Answer

18

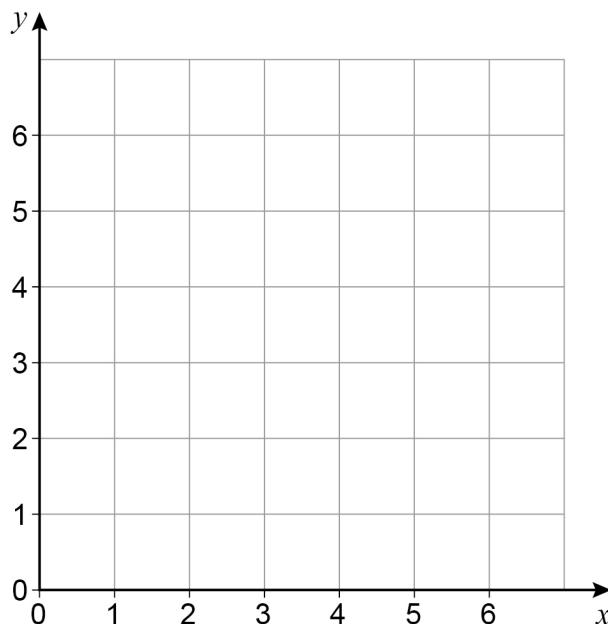
On the grid, identify the region represented by

$$x \leq 4 \quad y < 6 \quad x + y \geq 6$$

Label the region R.

**[3 marks]**

*Do not write  
outside the  
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**Turn over for the next question**

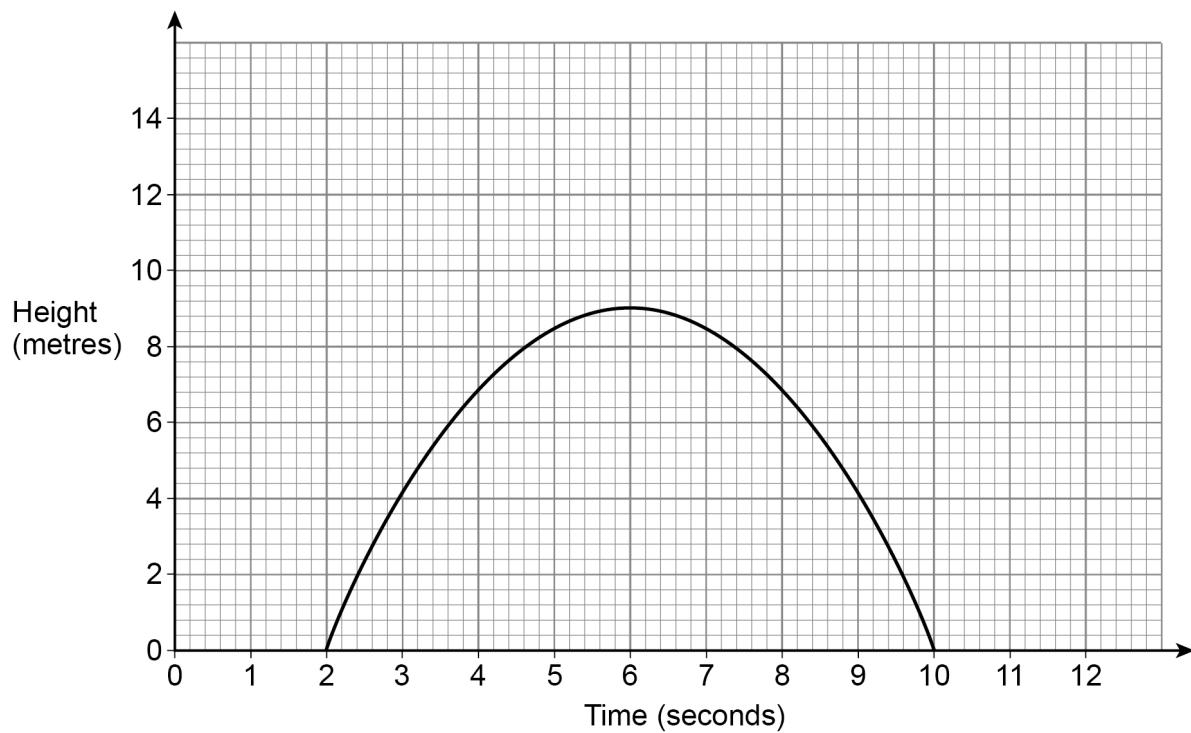
8

**Turn over ►**

19

The graph shows the height above ground of a toy rocket for 10 seconds.

Do not write  
outside the  
box



19 (a) For how long is the rocket in the air?

Circle your answer.

**[1 mark]**

10 seconds

8 seconds

5 seconds

2 seconds

19 (b) Using the graph, estimate the speed of the rocket after 4 seconds. State the units of your answer.

[3 marks]

## Answer

**20** A square has an area of 1.44 square centimetres.

Circle the length, in **millimetres**, of one side of the square.

**[1 mark]**

1.2 mm

12 mm

120 mm

1200 mm

**Turn over for the next question**

21

$x$  is an integer.

Prove that  $(3x - 1)^2 - 2x(4x + 2) + 24$  is a square number.

[4 marks]

*Do not write outside the box*

**22** Maria is trying to remember a 3-digit password using the digits 1–9.

She knows the rule that

the first digit is an even number  
the second digit is a factor of 18  
the third digit is a square number.

Maria tries at random a password that matches the rule.

Work out the probability that this is the correct password.

[4 marks]

## Answer

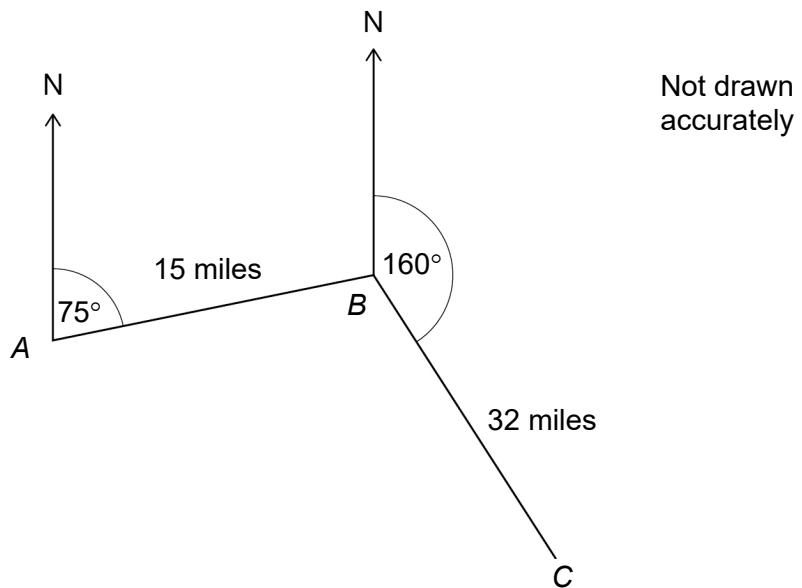
23

A ship sails from  $A$  to  $B$  and then from  $B$  to  $C$ .

$B$  is 15 miles from  $A$ , on a bearing of  $075^\circ$

$C$  is 32 miles from  $B$ , on a bearing of  $160^\circ$

Do not write  
outside the  
box



Work out the direct distance from  $A$  to  $C$ .

**[4 marks]**

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Answer \_\_\_\_\_ miles

24

The journey of a train was in two stages.  
The table shows information about the journey.

	Distance (km)	Speed (km/h)	Time (hours)
<b>1st stage</b>	306	$x - 16$	$\frac{306}{x - 16}$
<b>2nd stage</b>	550	$x$	$\frac{550}{x}$

In total, the journey lasted 4 hours.

Work out the value of  $x$ .

[5 marks]

## Answer

9

**Turn over ►**

**25** The equation of a curve is  $y = x^2 - 12x + 32$

By completing the square, work out the coordinates of the turning point.

You **must** show your working.

[3 marks]

Answer ( \_\_\_\_\_, \_\_\_\_\_ )

**END OF QUESTIONS**

**There are no questions printed on this page**

*Do not write  
outside the  
box*

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ANSWER IN THE SPACES PROVIDED**

Question number	<p style="text-align: center;"><b>Additional page, if required.</b> <b>Write the question numbers in the left-hand margin.</b></p>

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