

Please write clearly, in block capitals.

Centre number

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Candidate number

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Surname

Forename(s)

Candidate signature

GCSE MATHEMATICS

H

Higher Tier Paper 3 Calculator

Time allowed: 1 hour 30 minutes

Materials

For this paper you must have:

- mathematical instruments
- a calculator.



Instructions

- Use black ink or black ball-point pen. Draw diagrams in pencil.
- Answer **all** questions.
- You must answer the questions in the spaces provided. Do not write outside the box around each page or on blank pages.
- Do all rough work in this book. Cross through any work you do not want to be marked.

Information

- The marks for questions are shown in brackets.
- The maximum mark for this paper is 80.
- You may ask for more answer paper, graph paper and tracing paper. These must be tagged securely to this answer book.

Advice

- In all calculations, show clearly how you work out your answer.

For Examiner's Use

Pages	Mark
2 - 3	
4 - 5	
6 - 7	
8 - 9	
10 - 11	
12 - 13	
14 - 15	
16 - 17	
18	
TOTAL	

1 (a) Simplify $(x^3)^2$

[1 mark]

Answer _____

1 (b) Simplify $\frac{y^8}{y^2}$

[1 mark]

Answer _____

2 Write down the sum of the **exterior** angles of any polygon.

[1 mark]

Answer _____

3 $y = \frac{5\sqrt{x}}{2}$

Work out the expression for y^2

[2 mark]

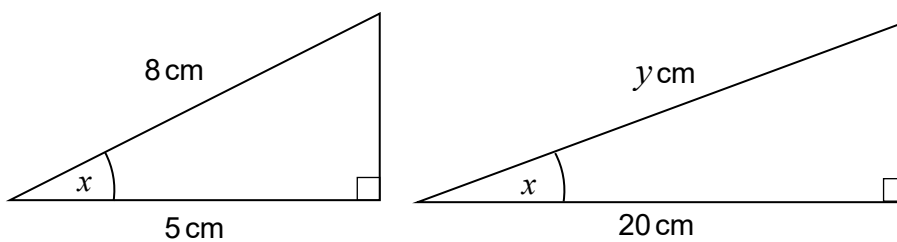
Answer _____

- 4 A time of 10.4 seconds is given to the nearest 0.1 of a second.
Complete the error interval.

[2 marks]

Answer _____ $\leq t <$ _____

- 5 These two right-angled triangles are similar.

Not drawn
accurately

- 5 (a) Write down the value of $\cos x$
Give your answer as a fraction.

[1 mark]

Answer _____

- 5 (b) Work out the value of y

[2 marks]

Answer _____ cm

- 6** In a band with 3 members, the mean age is 21 years old.
Ashley joins the band.
The mean age of **all** 4 members of the band is now 22 years old.
Work out the age of Ashley.

[4 marks]

Answer _____ years old

7 John chooses a number at random from the digits 1 to 4
Matt also chooses a number at random from the digits 1 to 4

7 (a) Write down the probability that the **total** of the two numbers chosen is 10

[1 mark]

Answer _____

7 (b) Work out the probability that the **total** of the two numbers chosen is more than 6

[3 marks]

Answer _____

8

At a cinema

3 adult and 2 child tickets cost £46

1 adult and 2 child tickets cost £24

Work out the cost of an adult ticket and the cost of a child ticket.

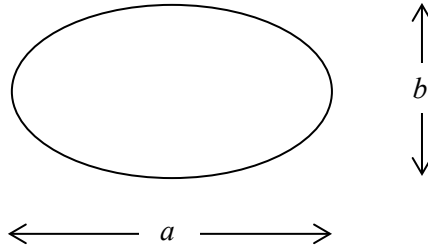
[3 marks]

Cost of an adult ticket £ _____

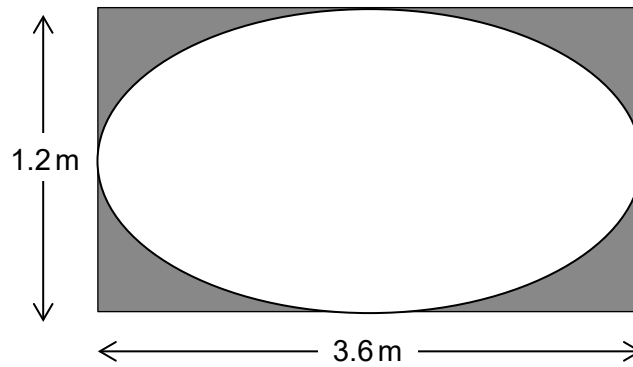
Cost of a child ticket £ _____

- 9 The area of an ellipse, width a and height b , is given by

$$\text{Area} = \frac{\pi ab}{4}$$



A sign is made from a rectangular metal sheet measuring 3.6 m by 1.2 m



Not drawn
accurately

The shaded sections are removed to make the sign.

Work out the percentage of the rectangular metal sheet used to make the sign.

[3 marks]

Answer _____ %

10

Company A claims that their products are half as likely to be faulty compared to Company B.

In a sample, 4% of products from Company A were faulty.

Here are the results of a sample from Company B.

Company B

	Number of products
Faulty	32
Not faulty	368

Comment on Company A's claim.

You **must** show your working.

[3 marks]

11 A teacher asks Ami and Jak to convert 20 976 into standard form.

11 (a) Ami writes 20.976×10^3

What is wrong with Ami's answer?

[1 mark]

11 (b) Jak writes 2.0976×10^{-4}

What is wrong with Jak's answer?

[1 mark]

12 At a concert the ratio of men to women is 5 : 3

The ratio of women to children is 9 : 4

Show that more than half of the people at the concert are men.

[3 marks]

13 Solve $4x^2 + 7x - 3 = 0$

Give your answers to 2 decimal places.

[3 marks]

$x =$ _____

14 A calculator gives a value of π as 3.14159

An approximation for π is $\sqrt{\frac{40}{3} - \sqrt{12}}$

Show that the value of the approximation is within 0.01% of the calculator value.

[4 marks]

15 Rearrange $e = \frac{f+7}{6-f}$ to make f the subject.

[4 marks]

Answer _____

16 The region R satisfies the three inequalities

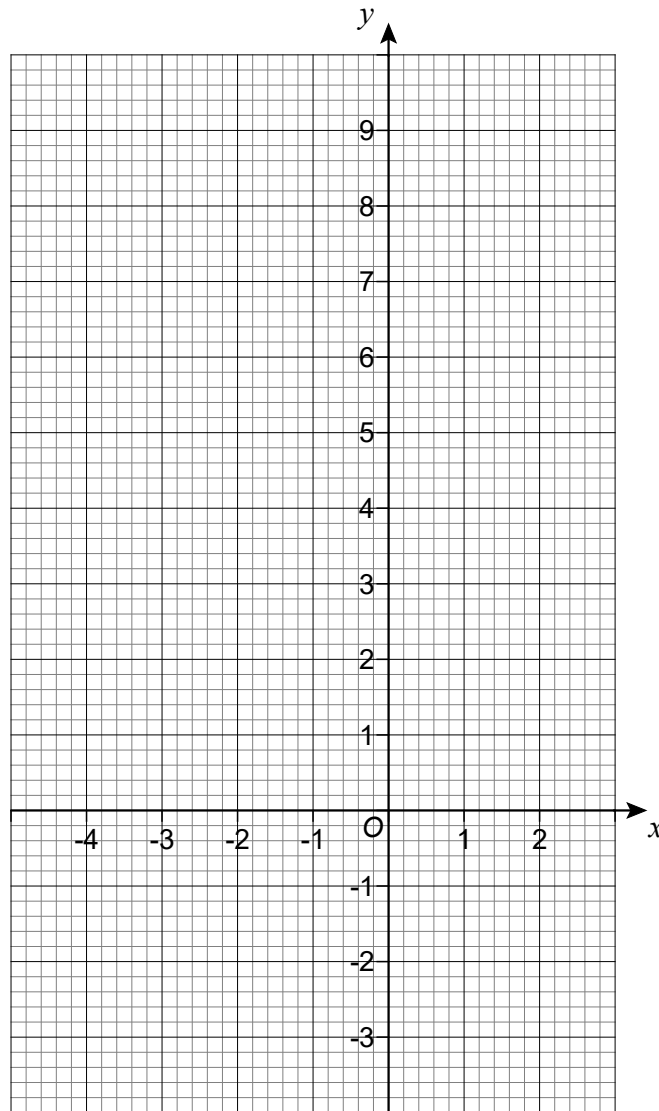
$$y < 3$$

$$x + y \geq 1$$

$$y \geq 2x - 2$$

Show the region R on the grid.

[4 marks]



17 The universal set contains the whole numbers 1 to 100

O is the set of odd numbers.

P is the set of prime numbers.

S is the set of square numbers.

17 (a) Explain why there are no numbers in $P \cap S$

[1 mark]

17 (b) How many numbers are there in $O \cup P$?

[1 mark]

Answer _____

18 a , b and c are three integers.

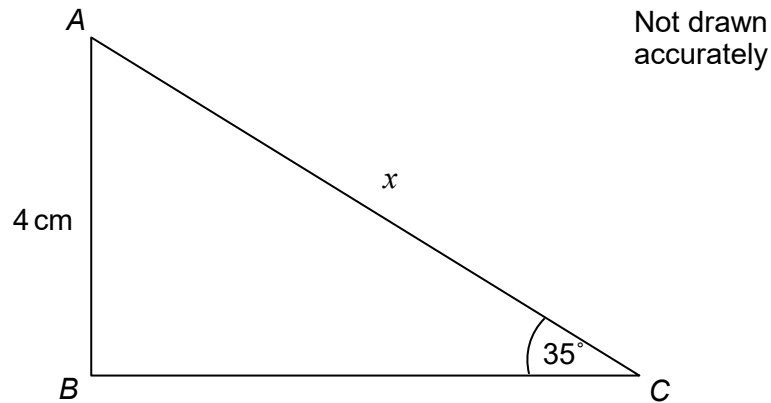
a is 5 less than b

c is 5 more than b

Prove that $ac + 25 = b^2$

[3 marks]

- 19** Nigel is using trigonometry to work out the size of length x .
He assumes that angle ABC is a right angle.



- 19 (a)** Using Nigel's assumption, work out the length x

[2 marks]

Answer _____ cm

- 19 (b)** In fact, angle ABC is 80°

How inaccurate does this make the answer to part (a)?

You **must** show your working.

[3 marks]

20

An object is dropped from a height h cm.
It takes T seconds to reach the ground.
 h is directly proportional to the square of T

When $h = 80$ $T = 4$

Work out the value of h when $T = 7.5$

[5 marks]

Answer _____

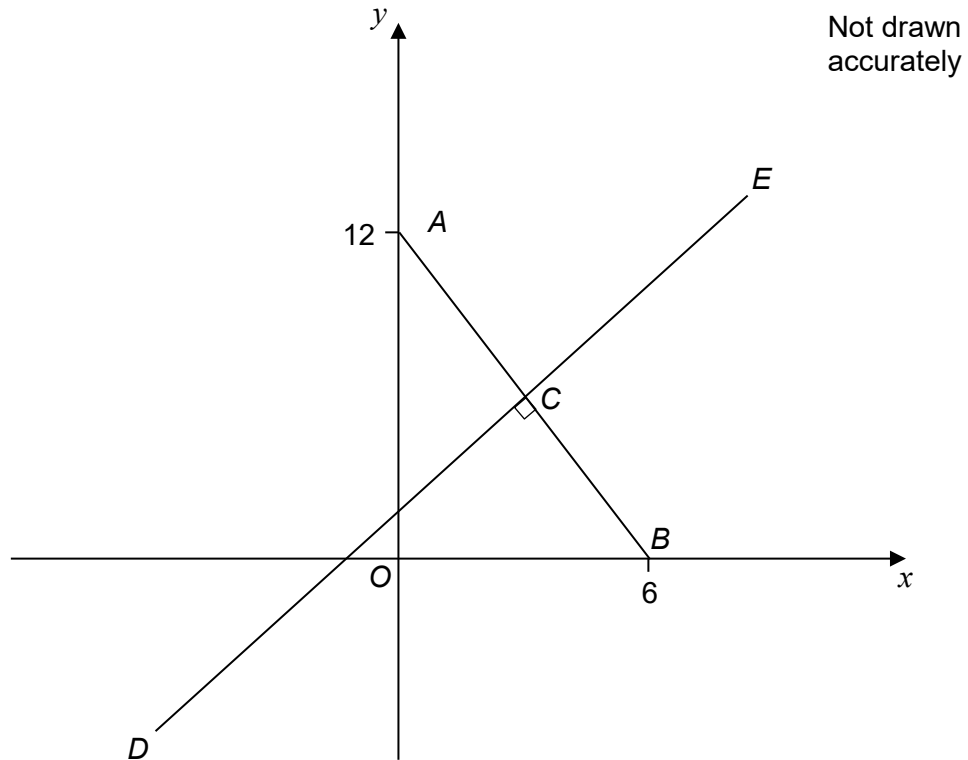
21

ACB is a straight line.

A is the point $(0, 12)$, and B is the point $(6, 0)$

C is the midpoint of AB .

Line DCE is perpendicular to line ACB .



Work out the equation of line DCE .

[5 marks]

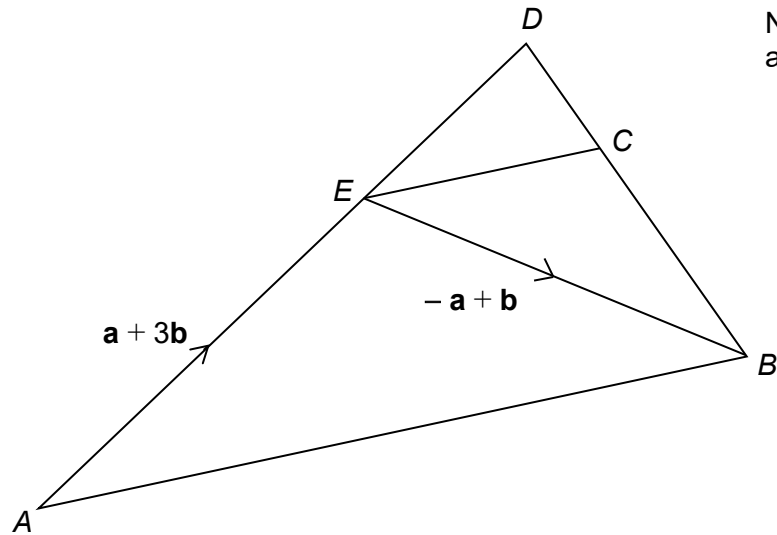
Answer _____

22

 AED is a straight line.

$$\vec{AE} = \mathbf{a} + 3\mathbf{b}$$

$$\vec{EB} = -\mathbf{a} + \mathbf{b}$$



22 (a)

Work out the vector \vec{AB}

[1 mark]

Answer _____

22 (b)

$$\vec{ED} = \frac{1}{3} \vec{AE} \quad \text{and} \quad \vec{DC} = -\frac{1}{3} \mathbf{a}$$

Prove that EC is parallel to AB .

[3 marks]

23

The graph with equation $y = x^2$ is translated by vector $\begin{pmatrix} 0 \\ -2 \end{pmatrix}$

Circle the equation of the translated graph.

[1 mark]

$$y = (x - 2)^2$$

$$y = (x + 2)^2$$

$$y = x^2 - 2$$

$$y = x^2 + 2$$

24

For all values of x , $f(x) = \frac{9x+4}{7}$

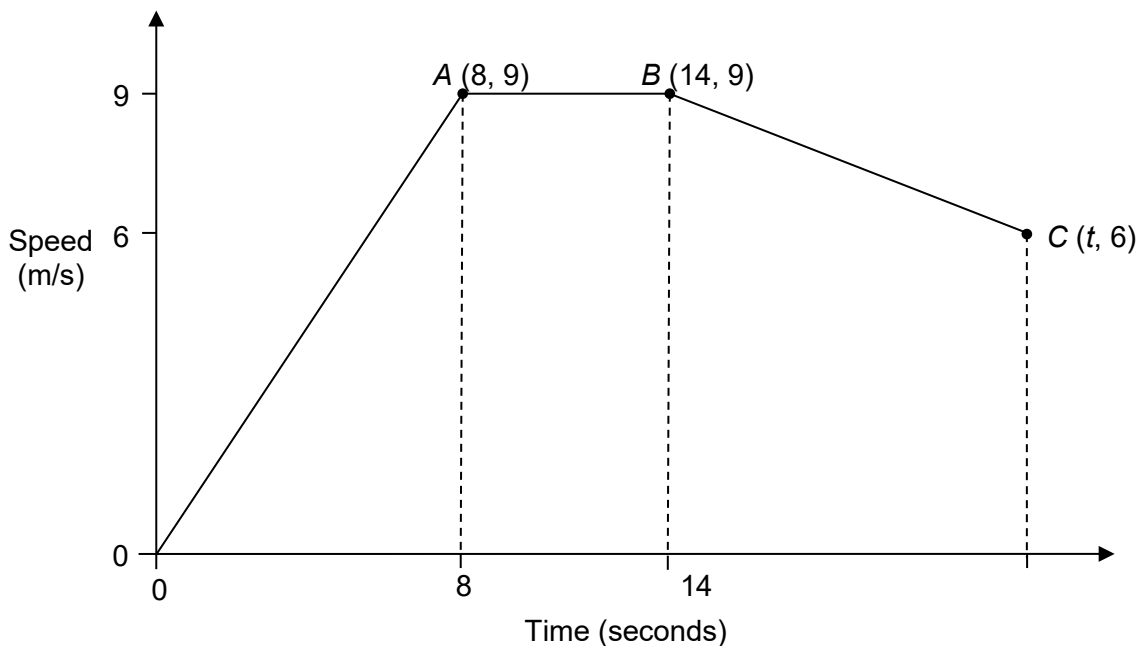
Work out $f^{-1}(x)$

[3 marks]

Answer _____

25

Here is a sketch of a speed-time graph for part of a journey.



The average speed from 0 to t seconds was 7.2 m/s

Work out the value of t

[5 marks]

Answer _____ seconds

END OF QUESTIONS

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