CALVERTON PRIMARY SCHOOL



CALCULATION POLICY

Person responsible for the policy	S Mintah Maths Lead
Date reviewed and shared with staff	May 2022
Date to be next reviewed by staff	May 2023
Date to be reviewed by the Local Governing Board	

Introduction

The purpose of this calculation policy is to provide guidance for the teaching of calculation methods in order to ensure consistency of practice in our schools and across the School. This policy is in accordance with The Primary National Curriculum in England. The strategies are with examples supporting a CPA approach, (Concrete, Pictorial, and Abstract). It is important to note that the concrete and representation examples are not exhaustive, and teachers and pupils may well come up with alternatives. For pupils to have a true understanding of a mathematical concept, they need to master all three phases of the CPA (concrete-pictorial-abstract) approach. This approach is explained below:

- Concrete the doing: A pupil is first introduced to an idea or a skill by acting it out with real objects. This is a 'hands on' component using real objects and it is the foundation for conceptual understanding. Concrete refers to objects such as base ten blocks, fraction tiles, markers, or other objects that can be physically manipulated.
- Pictorial the seeing: When a pupil has sufficiently understood the hands-on experiences performed, they can now relate them to pictorial representations, such as a diagram or picture of the problem.
- Abstract the symbolic: A pupil is now capable of representing problems by using mathematical notation, for example: $12 \div 2 = 6$. This is the most formal stage of mathematical understanding. Abstract representations can simply be an efficient way of recording the maths, without being the actual maths. They need to master all three phases.

Reinforcement is achieved by going back and forth between these representations. For example, if a child has moved on from the concrete to the pictorial, it does not mean that the concrete cannot be used alongside the pictorial. Or if a child is working in the abstract, 'proving' something or 'working out' could involve use of the concrete or pictorial. In short, these are not always 'exclusive' representations. Children should have a secure understanding before progressing onto the next step. Pupils who are successful should be challenged through rich problems rather than accelerating to the next stage unless it is deemed appropriate.

Mathematics Mastery

At the centre of the mastery approach to the teaching of mathematics is the belief that all children have the potential to succeed. They should have access to the same curriculum content and, rather than being extended with new learning, they should deepen their conceptual understanding by tackling challenging and varied problems. Similarly, with calculation strategies, children must not simply rote learn procedures but demonstrate their understanding of these procedures through the use of concrete materials and pictorial representations. This policy outlines the different calculation strategies that should be taught and used in EYFS linking to the updated curriculum 2021 and Year 6 in line with the requirements of the 2014 Primary National Curriculum.

Mathematical Language

High expectations of mathematical language development is essential, promoting mathematics as a language in itself that feeds into all elements of mathematics including reasoning. Teachers are expected to teach and understand all mathematical language related to the four operations and

this is clearly set out in the Federation mathematics vocabulary list as well as on the Calculations Policy. The National Curriculum is explicit in articulating the importance of children using the correct mathematical language as a central part of their learning (reasoning). Indeed, in certain year groups, the non-statutory guidance highlights the requirement for children to extend their language around certain concepts. It is therefore essential that teaching using the strategies outlined in this policy is accompanied by the use of appropriate and precise mathematical vocabulary. New vocabulary should be introduced in a suitable context (for example, with relevant real objects, apparatus, pictures or diagrams) and explained carefully. The school agreed list of terminology can be found attached and the discussion for reasoning questions are located as Appendix A to this policy.

EYFS Maths

The CPD federation approach to mathematics is based on the CPA method developed by American psychologist, Jerome Bruner.

Concrete

Concrete is the "doing" stage, using concrete objects to model problems.

Pictorial

Pictorial is the "seeing" stage, using representations of the objects to model problems.

Abstract

Abstract is the "symbolic" stage, where children are able to use abstract symbols to model problems. This approach develops children's understanding at a deeper level and helps children learn new ideas and build on their existing knowledge by introducing abstract concepts in a more

new ideas and build on their existing knowledge by introducing abstract concepts in a more familiar and tangible way.

Key Skills in Numbers (Birth to 3, 3-4, Reception):

- Recognise some numerals of personal significance.
- Recognises numerals 1 to 5.
- Counts up to three or four objects by saying one number name for each item.
- Counts actions or objects which cannot be moved.
- Counts objects to 10, and beginning to count beyond 10.
- Counts out up to six objects from a larger group.
- Selects the correct numeral to represent 1 to 5, then 1 to 10 objects.
- Counts an irregular arrangement of up to ten objects.
- Estimates how many objects they can see and checks by counting them.
- Uses the language of 'more' and 'fewer' to compare two sets of objects.
- Finds the total number of items in two groups by counting all of them.
- Says the number that is one more than a given number.
- Finds one more or one less from a group of up to five objects, then ten objects.

• In practical activities and discussion, beginning to use the vocabulary involved in adding and subtracting.

- Records, using marks that they can interpret and explain.
- Begins to identify own mathematical problems based on own interests and fascinations.

Early Learning Goal for Numbers:

- Children can count reliably with numbers from 1 to 20, place them in order and say which number is one more or one less than a given number.
- Using quantities and objects, they add and subtract 2 single-digit numbers and count on or back to find the answer.
- They solve problems, including doubling, halving and sharing.

Children must be exposed to different representations of mathematical concepts in order to embed conceptual understanding. One of the aims under the Characteristics of Effective Learning is 'creating and thinking critically.' Children are encouraged to make links, find new ways to do things, solve problems, change strategies as needed, make predictions, develop ideas of grouping, sequencing, cause and effect.

Addition EYFS

Children begin to combine groups of objects or pictures using concrete apparatus.

Solve simple problems using fingers.

Store the larger number mentally and use fingers to count on

Construct number sentences verbally or using cards to go with practical activities.

Children are encouraged to read number sentences aloud in different ways e.g. "Three add two equals 5" "5 is <u>equal</u> to three and two."

Count on to find the answer.

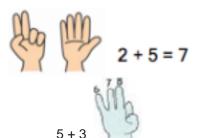
Have an understanding of what "more" means and be able to say what is one more than a given number.

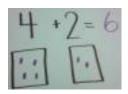
Number tracks can be introduced to count up on and to find one more.

Children make a record in pictures, words or symbols of addition activities.

When appropriate, Numicon shapes are introduced to identify 1 more/less, combine pieces to add and find number bonds.

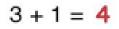
Number lines can be used alongside number tracks and practical apparatus to solve addition calculations and word problems.











Vocabulary:

Games and songs can be useful way to begin using vocabulary involved in addition. Add, more,

sum, and make, total, altogether.

MENTAL STRATEGIES: -

-Develop a mental image of the number system. -

-Understand the value of a number

-Counting forwards and backwards

-Recall of number bonds to 10

Addition Year 1

CPA Approach (Concrete, Pictorial, Abstract)

Counting and Combining sets of Objects to 20

Combining two sets of objects e.g. Numicon, bundles of straws, Dienes apparatus, multi-link cubes, bead strings, ten frames, etc., which will progress onto adding on to a set.

Understanding of counting using knowledge of number bonds

Ensure that children understand the combining and breaking up of a calculation (the part - part - whole relationship of numbers). 2+3=5 Represented using concrete linking to pictorial

From here move onto a bar model format so the children are used to grouping amounts together.

Understanding of counting on

(Supported by models and images). 7+4

If appropriate, progress from using number lines with every number shown to number lines with significant numbers shown. For example a number line that starts at 20 and finishes at 30

Children should be able to separate 2 digit numbers to add the ones then add the tens.

+ = signs and missing numbers

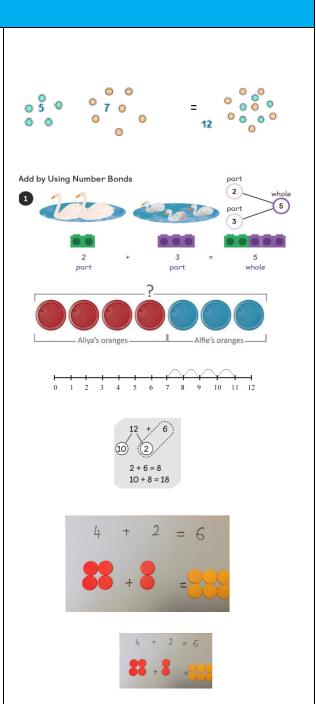
Children need to understand the concept of equality before using the '=' sign. Calculations should be written either side of the equality sign so that the sign is not just interpreted as 'the answer'.

$$2 = 1 + 1$$

2 + 3 = 4 + 1

This would be modelled well using resources to show that both sides are balanced

Children will solve one-step addition problems using concrete objects and/or pictorial representations



I have 4 sweets and I am given 2 more. How many do I have altogether?

Vocabulary

Add, Addition ,Total, Equal, Group, Calculation, Plus, Together

- MENTAL STRATEGIES: Know addition can be carried out in any order (commutative) Add 1 and 2 digit numbers to 20 including 0
- Number bonds to 20
- Doubles of numbers up to and including double 10Adding 10 to a single digit number
- Identify 1 more than a given number

Addition Year 2

CPA Approach (Concrete, Pictorial, Abstract)

It is valuable to use a range of representations (also see Y1). Continue to use objects, number lines and ten frames to develop understanding of commutative law and of:

Counting on in tens and ones

23 + 12 = 23 + 10 + 2= 33 + 2 = 35

Partitioning and bridging through 10.

The steps in addition often bridge through a multiple of 10

E.g. Children should be able to partition the 7 to relate adding the 2 and then the 5.

8 + 7 = 15 (8+2+5=15) Use Cube

Bar Modelling

Use of two parts making one whole through bar modelling. This can be shown using cubes as well as drawn.

This will support your pictorial element

Towards a Written Method

Partitioning in different ways and recombine to 100

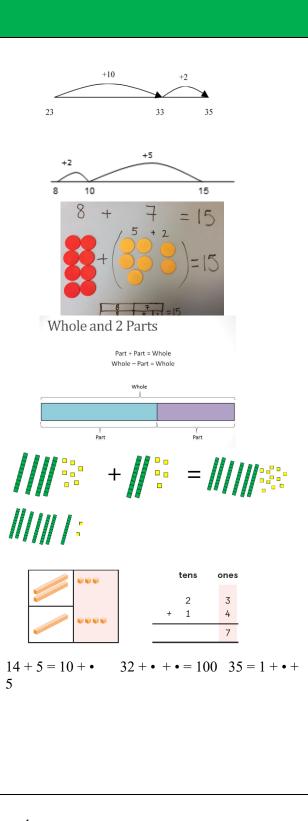
Leading towards Exchanging

Standard column method:

Concrete and pictorial to support the teaching of this method. Use of resources a necessity

Missing number problems

Vocabulary



Add, Addition, Total, Equal, Group, Calculation, altogether

MENTAL STRATEGIES:

- Know that addition is the inverse of subtraction

- Add numbers mentally, including:

A 2-digit number and units

A multiple of 10 to a 2-digit number T

wo 2-digit numbers

Three 1-digit numbers

- Use knowledge of inverse to check calculations and solve missing number problems

- Use knowledge of number bonds to 10 to calculate numbers bonds to 100

- Count on in tens from any given number (e.g 19 - 29 - 39 - 49 etc)

Addition Year 3

CPA Approach (Concrete, Pictorial, Abstract)

Bar Modelling

Bar Model approaches which will be continually referred to throughout the year to support the visual pictorial stage.

Children need to be secure adding multiples of 100 and 10 to any three-digit number including those that are not multiples of 10.

<u>Base 10</u>

Use of Base ten to support concrete and pictorial

Partition into tens and ones

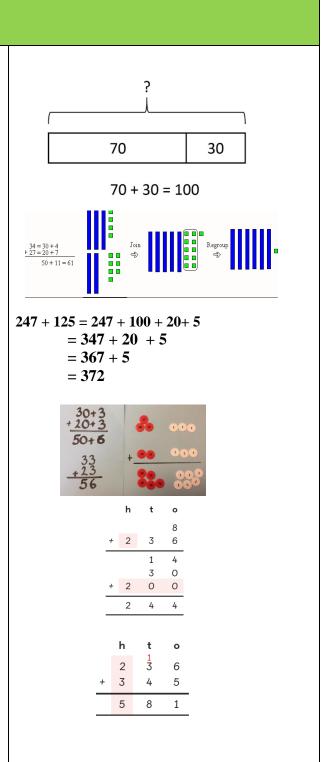
Partition both numbers and recombine. Count on by partitioning the second number only e.g.

Towards a Written Method to 1000

Standard column addition can be modelled with place value counters, objects and pictorial representations

Leading to children understanding the renaming between tens and ones (carrying/exchanging).

Include the Bar Method (See Above). Missing number problems using a range of equations as in Year 1 and 2 but with appropriate, larger numbers



Vocabulary Addend, Total, Sum, Partition, increase, altogether

MENTAL STRATEGIES:

- Add numbers mentally, including:
- a three-digit number and a single digit number

a 3-digit number and multiples of 10

- a 3-digit number and multiples of 100
- Estimate the answer to a calculation and use inverse operations to check answers
- Know number pairs that total 1000 (multiples of 100) Calculate 10 or 100 more than any given number

Addition Year 4

CPA Approach (Concrete, Pictorial, Abstract)

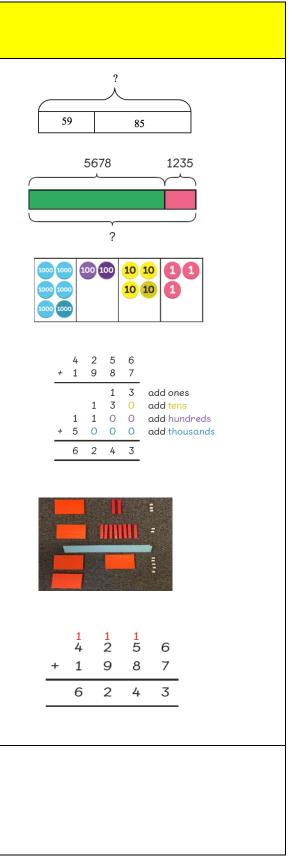
Mental methods (within 10,000)

This can be taught alongside methods such as Bar Modelling so that the children have a visual representation

Written methods (progressing to 4digits & 1dp)

Continue to model column addition with place value counters, objects, pictorial representations and the Bar Method

Ensure in the early stages you support as much as possible using resources to support calculations.



Regrouping

Extend to numbers with at least four digits, including renaming between various columns (Regrouping).

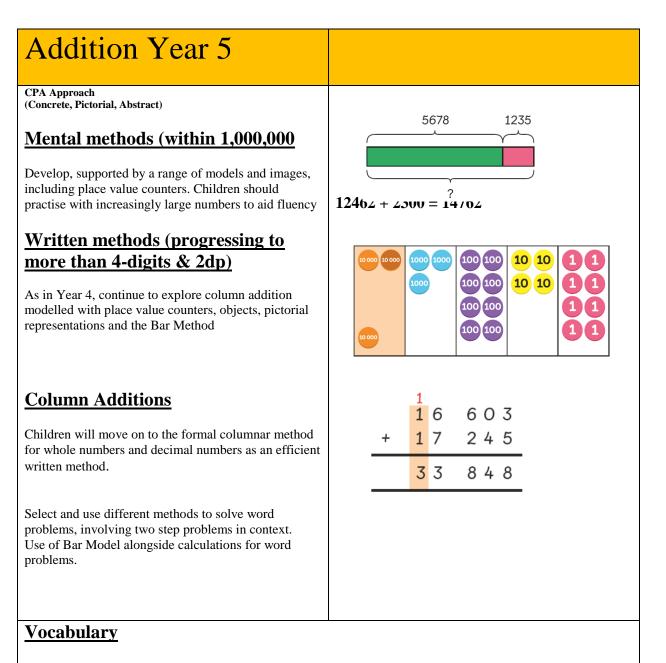
Select and use different methods to solve word problems, involving two step problems in context

Vocabulary

Addend, Total, Sum, Partition, increase, altogether

MENTAL STRATEGIES:

- Add numbers mentally, including:
a four digit number and multiples of one thousand
- Use knowledge of doubles to derive related facts (e.g
15 + 16 = 31 because $15 + 15 = 30$ and $30 + 1 = 31$)
- Know number pairs that total 1000 (multiples of 10)
- Estimate the answer to a calculation and use inverse
operations to check answers



Addend, Total, Sum, Partition, increase, altogether, exchange

Addition Year 6

CPA Approach (Concrete, Pictorial, Abstract)

Mental methods

Should continue to develop, supported by a range of models and images, including the number line. Including negative numbers and decimals

Written methods

As in Year 5, progressing to larger numbers, aiming for both conceptual understanding and procedural fluency with columnar method to be secured. Continue to model with place value counters, objects, pictorial representations and the Bar Method (See Appendix 1) Continue calculating with decimals, including those with different numbers of decimal places, and develop procedural fluency with renaming (carrying) to be secured.

Problem Solving

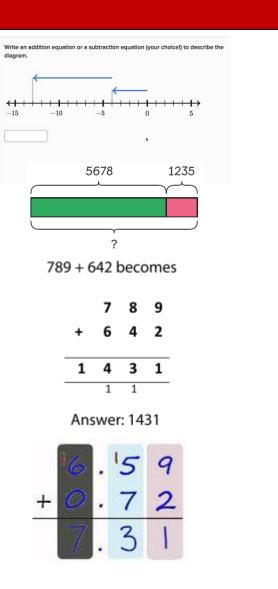
Teachers should ensure that pupils have the opportunity to apply their knowledge in a variety of contexts and problems (exploring cross curricular links) to deepen their understanding

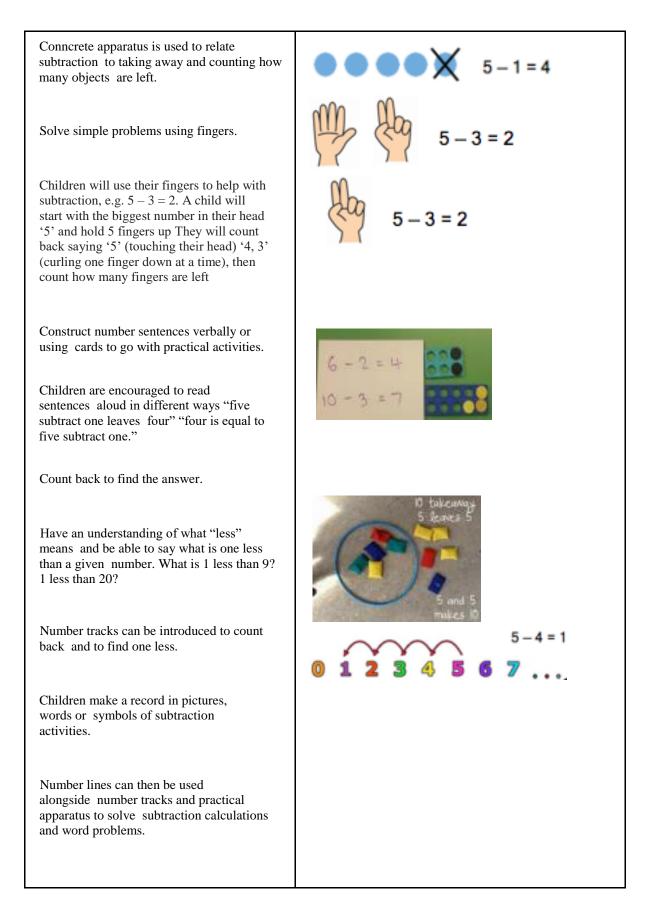
Refer to Year 5 for support with development groups.

Vocabulary

Addend, Total, Sum, Partition, increase, altogether

Subtraction EYFS



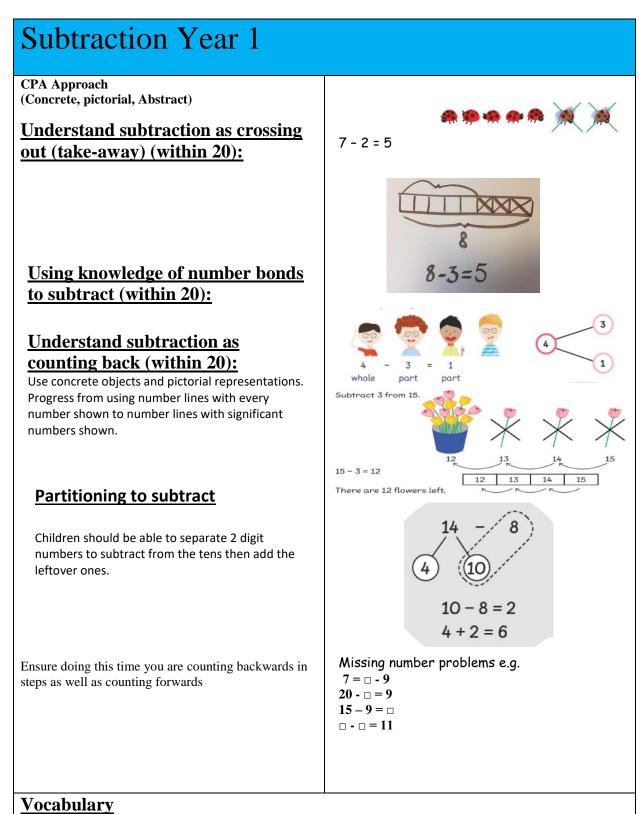


Vocabulary:

Games and songs can be a useful way to begin using the vocabulary involved in subtraction. Take (away), leave, left/left over, less, fewer, difference.

MENTAL STRATEGIES:

- Develop a mental image of the number system
- Children count backwards using familiar number rhymes (e.g '10 Green Bottles', '5 Fat Sausages')
- Count backwards from different starting points



Subtraction, Subtract, Take Away, Minus, Less, Backwards,

MENTAL STRATEGIES:

- Subtract 1 and 2 digit numbers to 20 including 0 - To know that subtraction is not commutative and that the larger number must always come first - Use knowledge of number bonds to 10 and 20 to reason (9 + 1 = 10 so 10 - 9 = 1 and 10 - 1 = 9)

Subtraction Year 2

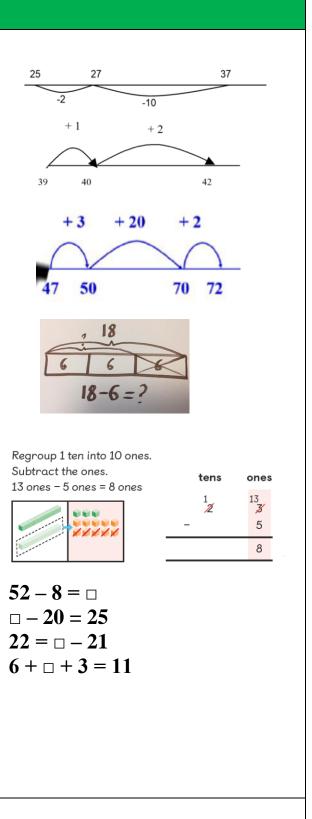
CPA Approach (Concrete, Pictorial, Abstract)

Recall and use subtraction facts to 20 fluently

It is valuable to use a range of representations (also see Y1). Continue to use Base Ten, number lines, ten frames and objects to model take-away and difference.

The link between the two may be supported by an image like this, with 47 being taken away from 72, leaving the difference, which is 25. Using number lines that do not need to go to 0

Bar Modelling by crossing out from the total



Towards written methods within 100

Record addition and subtraction in columns, the numbers may be represented with objects and pictorial representations. E.g. 23 – 5. Progress to renaming (borrowing).

Missing number problems, including use of inverse relationships

Vocabulary

Subtraction, Subtract, Take Away, Minus, Less, Backwards, inverse

MENTAL METHODS:

To know that subtraction is the inverse of addition

- Use knowledge of inverse to check calculations and solve missing number problems

- Subtract numbers mentally, including:

subtracting units from a 2-digit number

subtracting a multiple of 10 from a 2-digit number

subtracting a 2-digit number from another 2-digit number

- Recall and use subtraction facts to 20 fluently

- Use knowledge of number bonds to 100 (multiples of 10) to reason (40 + 60 = 100 so 100 - 60 = 40 and 100 - 60 = 40 and

40 = 60)

Subtraction Year 3

CPA Approach (Concrete, pictorial, Abstract)

Mental methods

Should continue to develop, supported by a range of models and images, including the number line Children should make choices about which strategy to use, depending on the numbers involved.

This will **lead** to renaming (borrowing), modelled using place value counters or Base Ten

Bar Model

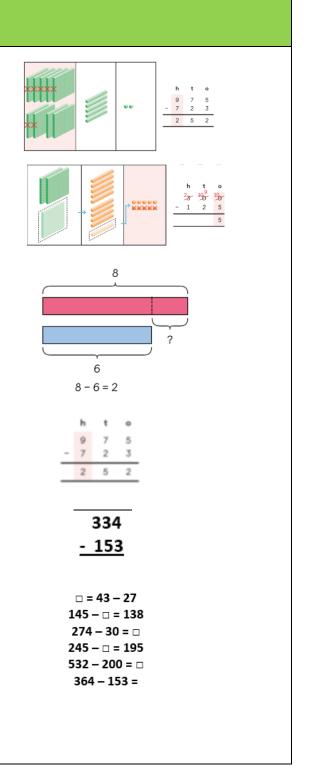
To show visualisation of subtraction problem

Written methods (progressing to 3digits)

Continue to model column subtraction with no renaming (Regrouping/decomposition), modelled with objects such as place value counters, Numicon and Base ten.

3 digit - 3 digit with tens value in subtrahend being greater - exchange from hundreds (no zero place values)

Missing number problems, including use of inverse relationships e.g.



Vocabulary Subtraction, Subtract, Take Away, Minus, Less, Backwards, inverse Subtrahend (amount being taken away) Minuend (the quantity from which another will be subtracted) Difference.

Subtraction Year 4

CPA Approach

(Concrete, pictorial, Abstract)

Mental methods (within 10,000)

Children should continue to develop, supported by a range of models and images, including partitioning.

Bar Model

To support the visualisation of subtraction. The missing element as a question mark

Written methods (progressing to 4-digits & 1 dp)

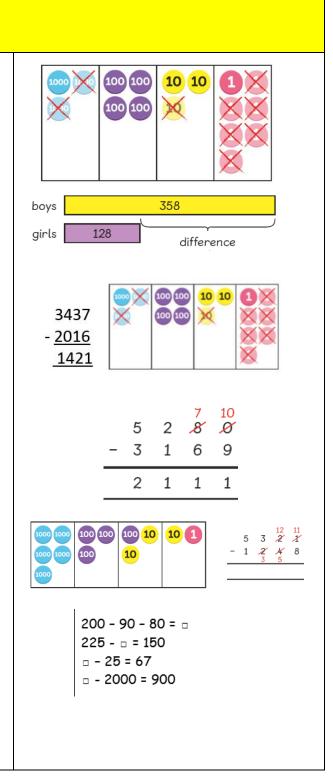
Continue to use column subtraction modelled with place value counters, objects, pictorial representations and the Bar Method (See Appendix 1)

Extend to numbers with at least four digits, including renaming between various columns (borrowing).

Use place value counters to explore compensation method

Select and use different methods to solve word problems,

Involve two step problems in context. Missing number/digit problems, including use of inverse relationships:



Vocabulary

Subtraction, Subtract, Take Away, Minus, Less, Backwards, inverse Subtrahend (amount being taken away) Minuend (the quantity from which another will be subtracted)

Subtrahend (amount being taken away) Minuend (the quantity from which another will be subtracted) Difference.

MENTAL STRATEGIES:

Subtract numbers mentally, including:

- Subtracting multiples of one thousand from a 4-digit number
- Use of number pairs that total 1000 (multiples of 10) to calculate subtraction (e.g 1000 300 = 700)
- Estimate the answer to a calculation and use inverse operations to check answers

Subtraction Year 5

CPA Approach (Concrete, pictorial, Abstract)

Mental methods (within 1 000 000) should continue to develop, supported by a range of

models and images, including partitioning.

Written methods (progressing to more than 4-digits)

As in Year 4, continue to use place value counters to support understanding of decomposition (renaming/excanging) in formal written method. E.g. 96 420 - 87 531 =

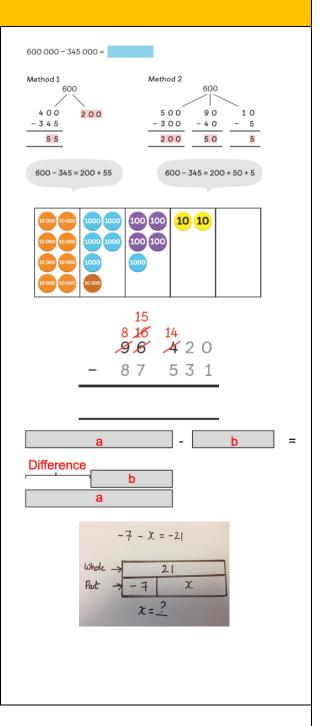
Continue to select and use different methods to solve word problems, involving two step problems in context.

Bar Model to support problem solving

Use of bar model for missing number problems; questions with more than one answer; Numbers involving negatives.

Missing number/digit problems:

 $6.45 = 6 + 0.4 + \Box;$ $119 - \Box = 86; 1\ 000\ 000 - \Box = 999\ 000;$ $600\ 000 + \Box + 1000 = 671\ 000; 12\ 462 - 2\ 300 =$



Vocabulary

Subtraction, Subtract, Take Away, Minus, Less, Backwards, inverse Subtrahend (amount being taken away) Minuend (the quantity from which another will be subtracted) Difference

MENTAL STRATEGIES:

Subtract increasingly large numbers mentally (e.g 12, 654 - 1,341 = 11, 213)

- Mentally subtract tenths (e.g 0.7 - 0.5 = 0.2) and 1-digit whole numbers and tenths (8 - 0.3 = 7.7) - Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy

Subtraction Year 6

CPA Approach (Concrete, pictorial, Abstract)

Mental methods

should continue to develop, supported by a range of models and images,

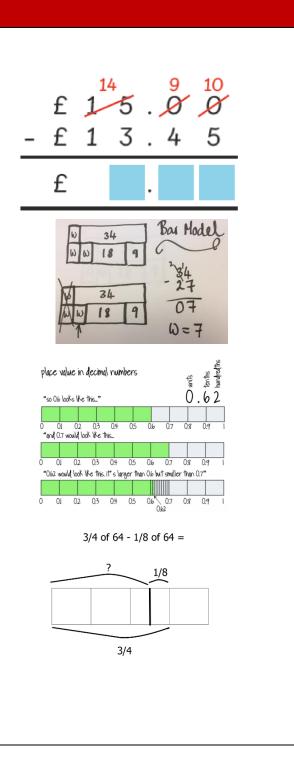
Written methods Alongside visual methods such as Bar Modelling

As in Year 5, progressing to larger numbers, aiming for both conceptual understanding and procedural fluency with columnar method to be secured. Continue to model with place value counters, objects, pictorial representations and the Bar Method.

Continue calculating with decimals, including those with different numbers of decimal places, and develop procedural fluency with decomposition (Regrouping) to be secured.

Problem Solving

Teachers should ensure that pupils have the opportunity to apply their knowledge in a variety of contexts and problems (exploring cross curricular links) to deepen their understanding



Vocabulary

Subtraction, Subtract, Take Away, Minus, Less, Backwards, inverse

Subtrahend (amount being taken away) Minuend (the quantity from which another will be subtracted) Difference, Zero digit

The year group markings relate to Mental Arithmetic sessions.

MENTAL STRATEGIES:

Subtract increasingly large numbers mentally (e.g 12, 654 - 1,341 = 11, 213)

- Mentally subtract tenths (e.g 0.7 - 0.5 = 0.2) and 1-digit whole numbers and tenths (8 - 0.3 = 7.7) - Use rounding to check answers to calculations and determine, in the context of a problem, levels of accuracy

Multiplication EYFS The link between addition and multiplication can be introduced through doubling and reinforced through repeated addition of the same number. 5 5 5 Numicon is used to visualise the repeated adding of the same number. Children begin with mostly pictorial representations e.g. How many groups of 2 are there? 2 + 2 + 2 + 2 + 2 + 2, so 5 groups of 2. Real life contexts and use of practical equipment is used to count in repeated groups of the same size e.g. How many wheels are there altogether? Children are encouraged to read number sentences aloud in different ways "five times two makes ten" "ten is equal to five multiplied by two" "ten is the same as five lots of two." 2, 4, 6, 8, 10, 12 Count in twos, fives and tens both aloud and with objects. Children are given multiplication problems set in a real life context. Children are encouraged to visualise the problem e.g. How many fingers on two hands? How many sides on three triangles? How many legs on four ducks?

Vocabulary:

Lots of, groups of, times, repeated addition, double, combine.

MENTAL STRATEGIES:

Develop a mental image of the number system.

- Understand the value of a number
- Counting in 2s, 5s and 10s.
- Number patterns on a number line and on a hundred squares

– 2's, 5's and 10's.

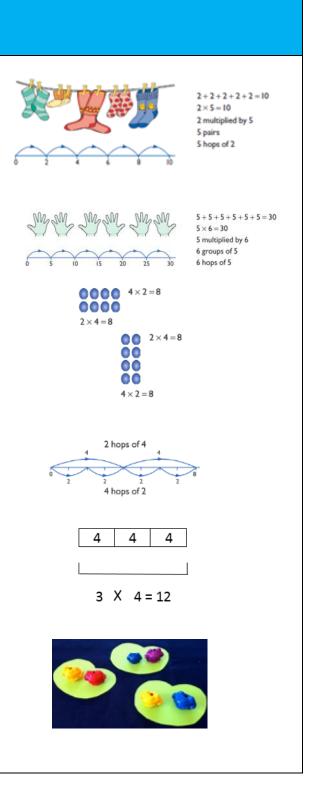
Multiplication Year 1

CPA Approach (Concrete, pictorial, Abstract)

Doubling and repeated addition

Understand multiplication is related to doubling and combing groups of the same size (repeated addition) for 2, 5, 10.

Washing line, and other practical resources for counting. Concrete objects: Base Ten, Numicon, bundles of straws, bead strings



Bar Modelling

Use of bar model as a visual to support early multiplication. This can be taught through cubes or counters

Problem solving

Problem solving with concrete objects (including money and measures) Use arrays to begin to understand multiplication can be done in any order (commutative)

Vocabulary Groups of, times, multiply, addition, arrays, lots of

MENTAL STRATEGIES: Count forwards and backwards in multiples of 2s, 5s and 10s.

- Recall doubles of numbers up to and including 10.

Multiplication Year 2

CPA Approach (Concrete, Pictorial, Abstract)

Times table Facts

Recall and use multiplication facts for the 2, 5 and 10 multiplication tables as a minimum requirement Develop understanding of solving multiplication problems using arrays, objects, pictorial representations and number lines (see Year 1).

Number Sentences

Expressing multiplication as a number sentence using x and explore commutative law of multiplication

Scaling

Begin to develop understanding of multiplication as scaling (3 times bigger/taller)

Number lines

Using number lines with a link to repeated addition.

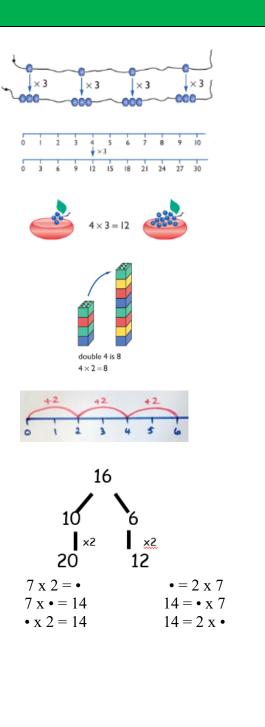
Doubling numbers up to 10 + 10

Link with understanding scaling Using known doubles to work out double 2 digit numbers (double 15 = double 10 + double 5)

Towards written methods

Use arrays and jottings to develop an understanding of doubling two digit numbers

Solve missing number problems.



Vocabulary

Groups of, times, multiply, addition, arrays, lots of, multiplication

MENTAL STRATEGIES:

- Count forwards and backwards in multiples of 3.
- Know the 2, 5 and 10 times tables (in and out of order)
- Recognise odd and even numbers

Multiplication Year 3

CPA Approach (Concrete, pictorial, Abstract)

Mental methods

Doubling 2 digit numbers using partitioning

Demonstrating multiplication on a number line – jumping in larger groups of amounts $13 \ge 4 = 10$ groups of 4 then 3 groups of 4

Recall and use multiplication facts for the 3, 4 and 8 multiplication tables

Bar modelling

Developing this method further to go alongside calculations

Written methods (progressing to 3digit x 1digit)

Developing written methods using understanding of visual images to group and create equal groups of objects and pictures

Grid method

2 and 3 digit by 1 digit only looking at partitioning of multiplicand

Short Multiplication

2 by 1 digit numbers using known facts to support

Vocabulary

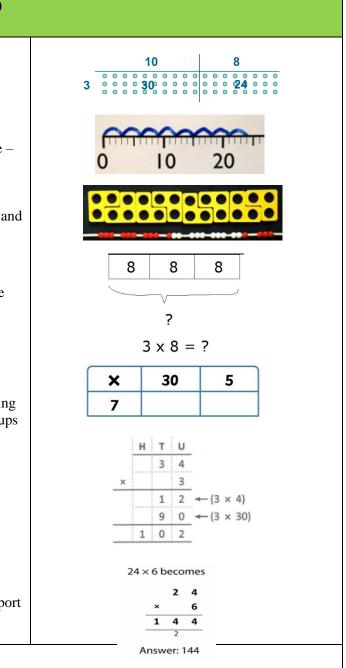
Multiplicand (Number to be multiplied) Multiplier (Amount that multiplicand is being multiplied by) Product, lots of, groups of, times, as much, factors

MENTAL STRATEGIES:

Count forwards and backwards in multiples of 4, 8, 50 & 100 - Know the 3, 4 and 8 times tables (in and out of order)

- Connect the 2, 4 and 8 times tables through doubling

- Use knowledge of place value to calculate multiplication (e.g. $2 \ge 4$, $2 \ge 4$, $2 \ge 40$, $2 \ge 400$)



Multiplication Year 4

CPA Approach (Concrete, pictorial, Abstract

Mental methods

Counting in multiples of 6, 7, 9, 25 and 1000, and steps of 1/100.

Recall and use multiplication facts for the 6, 7, 9, 11 and 12 multiplication tables Use known facts to multiply by multiples of 10

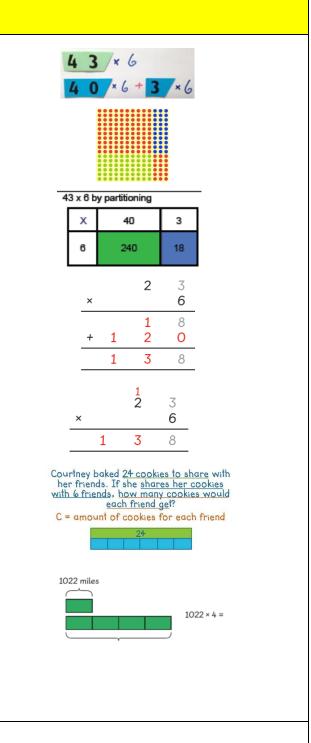
Written methods (progressing to 3digit x 2digit, including 1dp)

Children to embed and deepen their understanding to multiply up to 2d x 2d progressing to 3d x 2d and decimals to 1dp. Ensure this is still linked back to their understanding of arrays and supported using place value counters

Leading to short written method including regrouping (carrying):

Children to use their knowledge of multiplication tables and inverse, supported by pictorial representations and the Bar Method

Bar Model to support calculations and word problems



Vocabulary

Multiplicand (Number to be multiplied) Multiplier (Amount that multiplicand is being multiplied by) Product, lots of, groups of, times, as much, factors

MENTAL STRATEGIES:

Know all times tables up to and including 12 x 12 (by the end of Year 4)

- Recognise and use factor pairs (e.g factor pairs for numbers up to and including 10)
- Know that TU x 5 is TU x 10 then divide by 2 (e.g $18 \times 5 = (18 \times 10) \div 2 = 90)$
- Know that TU x 9 is TU x 10 then subtract TU (e.g $18 \times 9 = (18 \times 10) 18 = 162)$

Multiplication Year 5

CPA Approach

(Concrete, pictorial, Abstract)

Mental methods

X whole numbers and decimals by 10, 100, 1000 using knowledge of place value to move digits

Use practical resources and jottings to explore equivalent statements (e.g. $4 \times 35 = 2 \times 2 \times 35$)

Recall of prime numbers up to 19 and identify prime numbers up to 100 (with reasoning)

Identify multiples and factor pairs for numbers

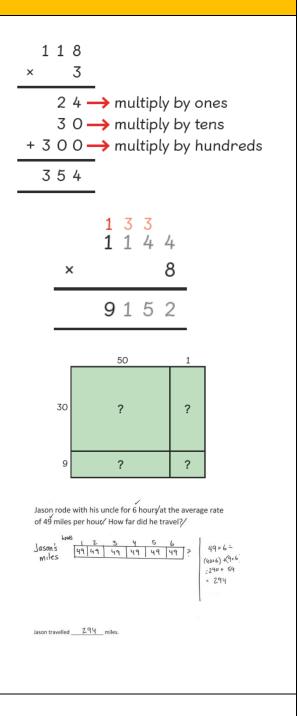
Written methods (progressing to 4d <u>x 2d)</u>

Children to continue to explore long and short methods:

As in Year 4, children to use their knowledge of multiplication tables and inverse, supported by pictorial representations and the Bar Method

Grid method to multiply 2 digit numbers by 2 digit numbers e.g. $39 \times 51 =$

<u>Bar model to support Problem</u> solving. Link with other operations



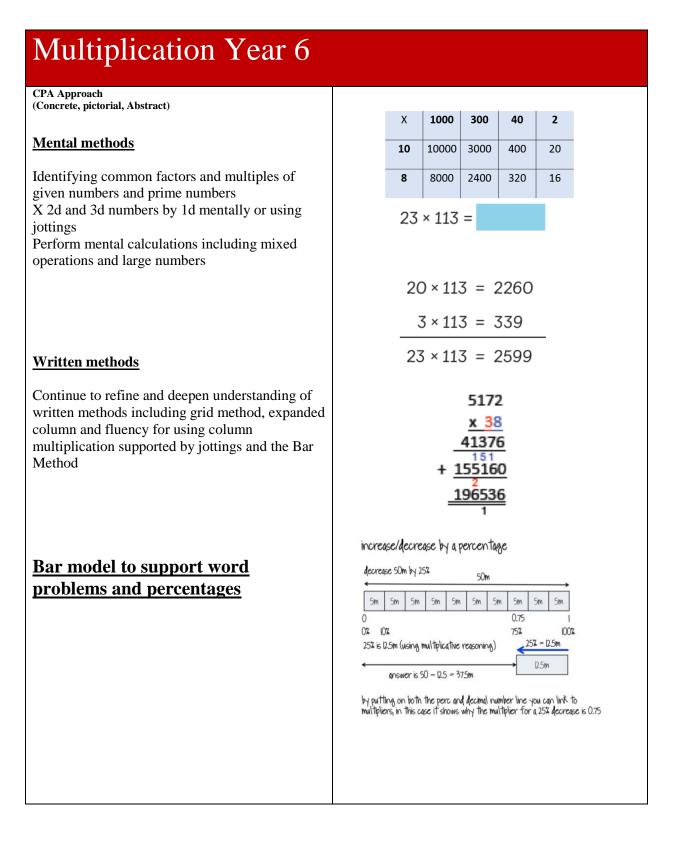
Vocabulary

Multiplicand (Number to be multiplied) Multiplier (Amount that multiplicand is being multiplied by) Product, lots of, groups of, times, as much, Factors

MENTAL STRATEGIES:

Recognise and calculate factor pairs for any number - Use times table knowledge to derive multiples of any number - Establish whether a number is a prime number (up to 100) or a composite number (not prime) and recall prime numbers up to 19

- To know what a square number is and recall all square numbers (up to and including 144)
- To know what a cube number is and recall the first 5 cube numbers



Vocabulary

Multiplicand (Number to be multiplied) Multiplier (Amount that multiplicand is being multiplied by) Product, lots of, groups of, times, as much, Factors

MENTAL STRATEGIES:

Use scaling to solve decimal number problems as whole number problems using the rule: 'the number of decimal digits in the question is the same as the number of decimal digits in the answer'

- Identify common factors, common multiples and prime numbers

- Use common factors to simplify fractions mentally

- Use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy

Calverton Primary School Calculation Policy: Multiplication

Division EYFS

Division can be introduced through halving or sharing an equal amount into 2 groups.

Children begin with mostly pictorial representations linked to real life contexts.

Children need to see and hear representations of division as both grouping and sharing.

<u>Grouping model:</u> Mum has 6 socks. She grouped them into pairs. How many pairs did she make?

Sharing model:

I have 10 sweets. I want to share them with my friend. How many will we have each?

The sharing model is a useful way to introduce young children to fractions e.g. Can you cut the pizza in half?

Children make a record in pictures, words or symbols of division activities.

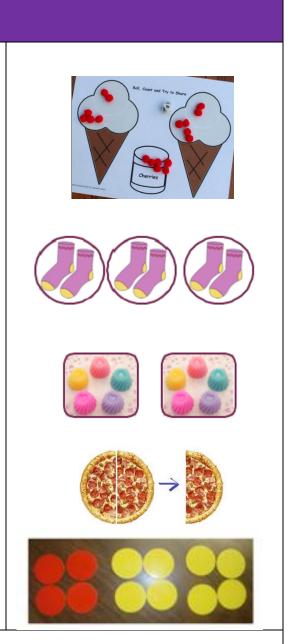
Children are encouraged to have a go at recording the calculation that has been carried out e.g. by arranging concrete objects into groups.

Vocabulary:

Half, halve, share, equal, groups of, left/left over.

MENTAL STRATEGIES:

Count forwards and backwards in multiples of 2s, 5s and 10s.



Division Year 1

CPA Approach (Concrete, pictorial, Abstract)

Number Patterns

Children must have secure counting skills- being able to confidently count in 2s, 5s and 10s. Children should be given opportunities to reason about what they notice in number patterns.

Group AND share small quantities to 10- understanding the difference between the two concepts. Sharing

Importance of one-to-one correspondence.

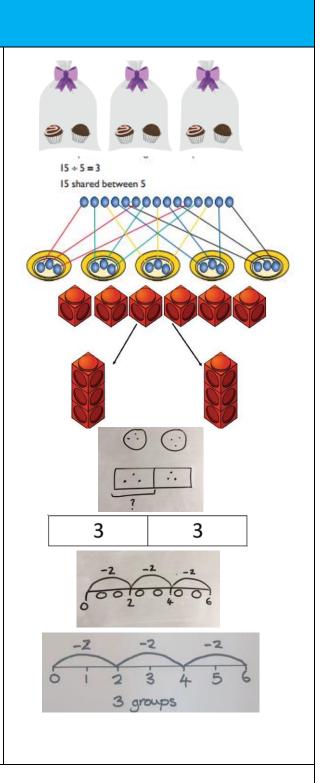
Children should be taught to share using concrete apparatus.

Grouping and Use of Bar Model

Children should apply their counting skills to develop some understanding of grouping. How many groups of 2 in 6?

Arrays as a pictorial representation can be used for division. $15 \div 3 = 5$ There are 5 groups of 3. $15 \div 5 = 3$ There are 3 groups of 5.

Children should be able to find ½ of shapes, objects, numbers and quantities.



Vocabulary

halve, share, share equally, groups, equal groups of, divide, divided by, left, left over <u>MENTAL STRATEGIES</u>:

Count forwards and backwards in multiples of 2s, 5s and 10s

Division Year 2

CPA Approach (Concrete, Pictorial, Abstract)

Sharing and Grouping

Know and understand sharing and groupingintroducing children to the \div sign. Recall and use division facts for the 2, 5 and 10 multiplication tables

Children should continue to use grouping and sharing for division (dividends below 20) using practical apparatus, arrays and pictorial representations.

<u>Progress to Grouping using a</u> <u>number line</u>

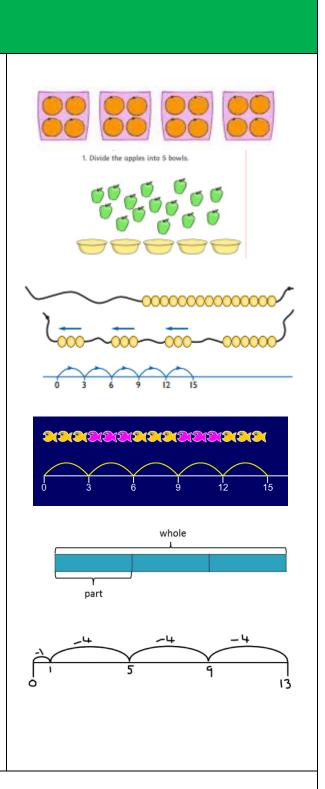
Group from zero in jumps of the divisor to find out 'how many groups of 3 are there in 15?'. $15 \div 3 = 5$

Bar Model

Using bar model to represent a number divided into $\frac{1}{2}$ $\frac{1}{4}$ etc. With not remainders at the start point.

Remainders using resources

Continue work on arrays. Support children to understand how multiplication and division are inverse. Look at an array – what do you see? Remainders can be introduced by use of number lines; sorting activities; cube and counter use and bar model.



Vocabulary

groups of, equal groups of, halve, share, share equally, divide, divided by, divided into, repeated subtraction, inverse.

MENTAL STRATEGIES:

To know that division is the inverse of multiplication

- Recall division facts for the 2, 5 and 10 times tables

- Recall halves for even numbers up to and including 20

Division Year 3

CPA Approach (Concrete, pictorial, Abstract)

Recall of Known facts

Recall and use division facts for the 3, 4 and 8 multiplication tables using times grids. Children should continue to use grouping and sharing for division using practical apparatus, arrays and pictorial representations.

Place value counters, arrays and number lines can be used to support children apply their knowledge of grouping.

Partitioning

Children need to be able to partition the dividend in different ways. $48 \div 4 = 12$

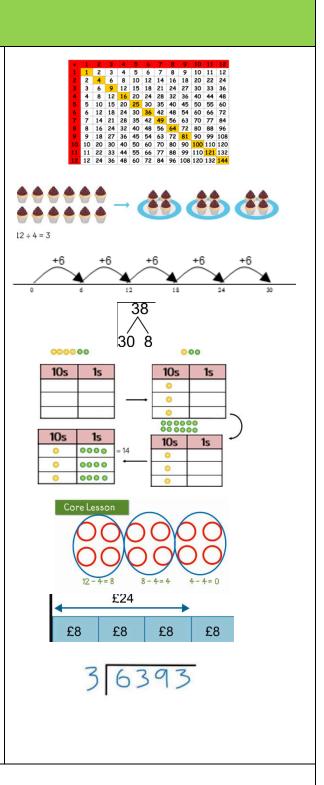
Bar Model and Short Division

Use of bar model as a representation to link alongside basic 2 digit short division. Starting with 2 digit dividends with no remainders moving onto remainders and showing remainder as a fraction

Repeated Subtraction

<u>÷ = signs and missing numbers</u>

Continue using a range of equations as in year 2 but with appropriate numbers.



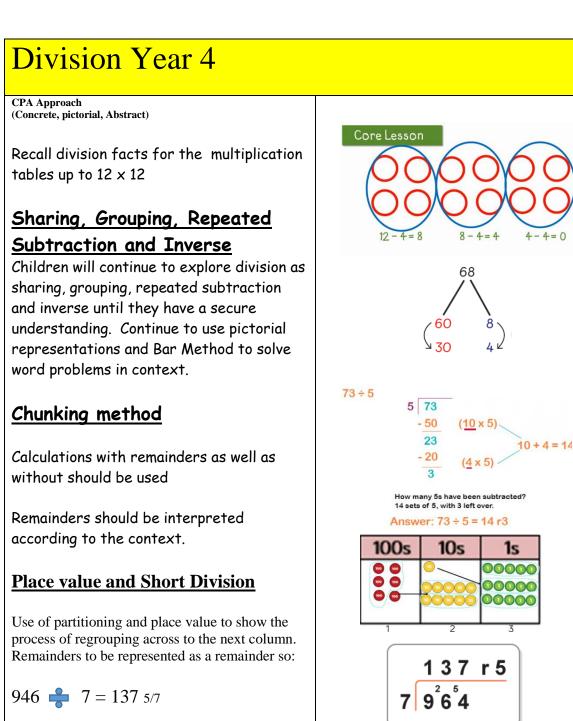
Vocabulary

Divisor, dividend, quotient, sharing, groups of, lots of, vinculum

MENTAL STRATEGIES:

Know the division facts from the 3, 4 and 8 times tables

- Use knowledge of place value to calculate division (e.g. $14 \div 2 = 7$, $140 \div 2 = 70$, $1400 \div 2 = 700$)

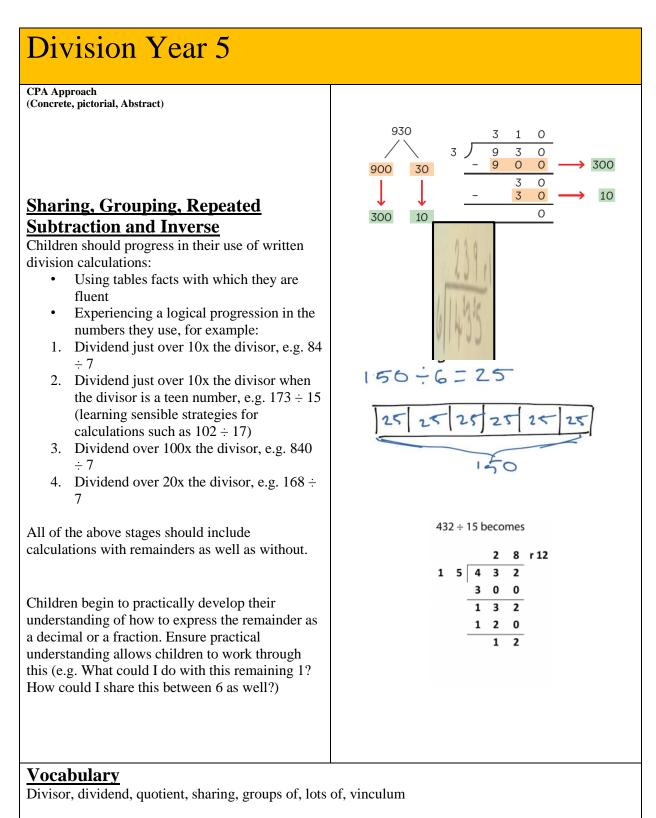


Vocabulary

Divisor, dividend, quotient, sharing, groups of, lots of, vinculum

MENTAL STRATEGIES:

Know all related division facts for all times tables up to 12 times table (by the end of Year 4)



MENTAL STRATEGIES:

Multiply and divide numbers mentally drawing upon known facts - Associate fractions with division

Division Year 6

CPA Approach

(Concrete, pictorial, Abstract)

Sharing, Grouping, Repeated **Subtraction and Inverse**

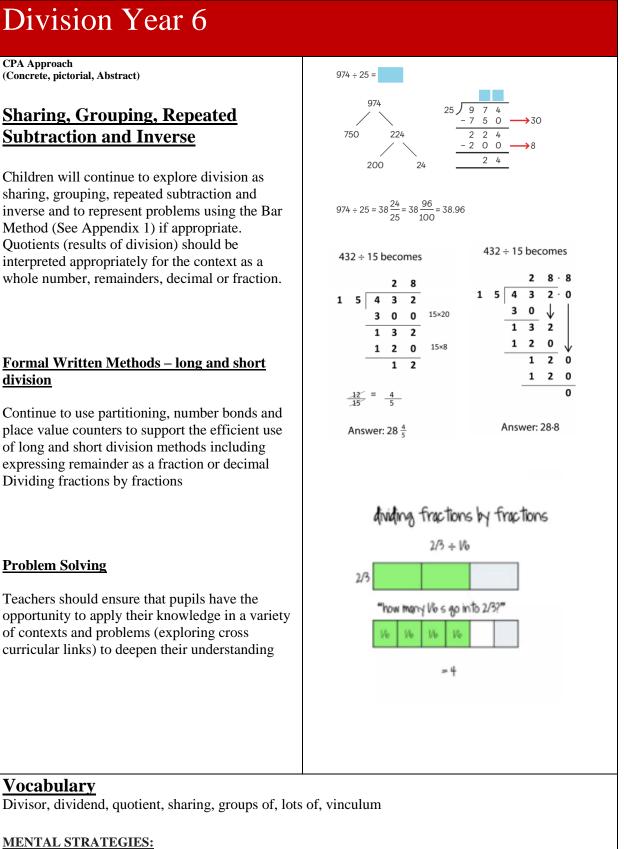
Children will continue to explore division as sharing, grouping, repeated subtraction and inverse and to represent problems using the Bar Method (See Appendix 1) if appropriate. Quotients (results of division) should be interpreted appropriately for the context as a whole number, remainders, decimal or fraction.

Formal Written Methods - long and short division

Continue to use partitioning, number bonds and place value counters to support the efficient use of long and short division methods including expressing remainder as a fraction or decimal Dividing fractions by fractions

Problem Solving

Teachers should ensure that pupils have the opportunity to apply their knowledge in a variety of contexts and problems (exploring cross curricular links) to deepen their understanding



MENTAL STRATEGIES:

Vocabulary

Use estimation to check answers to calculations and determine, in the context of a problem, levels of accuracy - Calculate a fraction of an amount

Appendix A

Mathematical Language:

High expectations of the mathematical vocabulary and language used are essential, with staff only accepting what is correct.

Consistency across the school is key:

Correct Terminology	Incorrect Terminology
Ones	Units
Is equal to (is the same as)	Equals
Zero	Oh (the letter 'o')
Exchange Exchanging Regrouping	Stealing Borrowing
Calculation Equation	Generic term of 'sum' or 'number sentence'
Whole (bar model) Part	

Encourage discussion and reasoning:

- > What do you notice?
- > True or false? Odd one out?
- > Do, then explain
- > Spot the mistake
- >> Give an example of
- > Continue the pattern
- > Convince me...prove it!
- > What is the same.....what is different?
- > Is this always, sometimes or never true? If sometimes, when?
- > If this is my answer, what could the question be?
- ➤ Explain why
- ➤ I wonder why
- > How do you know
- > Does anyone know
- > What will happen if

- > How will you know
- \gg How can we find out
- ➤ Can you describe ...?
- > Is there another way
- > What makes you think that ...?